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## Algebra 2H: Polynomial functions and transformations

## (Practice test)

Remember: The goal of this test is to enable you to demonstrate your knowledge of the material.

1. The test has $\underline{6}$ questions, plus one extra-credit question.
2. Total points available are 40 , plus 2 for extra credit.
3. You have 50 minutes (one block) to complete the test (more if you have accommodations).

Common test instructions:
4. You should SHOW YOUR WORK for all parts of the answer in order to receive full credit.
5. Write your answers using either Blue or Black ink or a pencil. Please don't use red pen.
6. Clearly indicate (underline/ box/highlight) your final answer. Mark only ONE answer per question.

Special note:
7. You need to finish all aspects of the test BEFORE 4pm, Friday, March-31 ${ }^{\text {st }}$.

If any of the above is problematic for you, please let me know BEFORE Wednesday, March $29^{\text {th }}$.

| The use of a graphing calculator is NOT allowed. |
| :---: | :---: |
| A simple 4-operations calculator is allowed. |

Good luck!!
Dr. Baharav

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## Question 1 ( 10 pts )

Given the expression:

$$
3 x\left(x^{2}-x\right)+x^{5}-x^{4}+4-4 x
$$

a) Write the polynomial in standard form $\mathrm{P}(\mathrm{x})=$ $\qquad$
b) How many terms are there in $\mathrm{P}(\mathrm{x})$ ?
c) What is the degree of the polynomial?
d) What is the sign of the leading coefficient?
e) What is the end behavior of the graph?
f) It is given that the polynomial has a root at $x=1$, and another root at $x=-2 \mathrm{i}$. Find the remaining roots of the polynomial.
g) Write the polynomial in a factored form.

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h) What is the y-intercept of the polynomial?
i) Utilizing all the information gathered above (and only this information), plot $\mathrm{P}(\mathrm{x})$ in the graph below.


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## Question 2 ( 6 pts)

a) Given the polynomial

$$
P(x)=x^{3}-x^{2}-2 x+2
$$

I. Find all possible rational roots
II. Find the roots of the polynomial
b) Given the polynomial

$$
P(x)=5 x^{9}-3 x^{4}+7 x^{3}+x-2
$$

I. Determine the number of possible positive real roots
II. Determine the number of possible negative real roots

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## Question 3 ( 6 pts)

For each of the below functions, write the domain and range of the function, and plot it on the axes below.
There will be multiple graphs on the same axes, so please indicate clearly which line corresponds to which item.
a. $f(x)=\sqrt{x}$

Domain: $\qquad$ Range: $\qquad$
b. $f(x)=\sqrt{(x-2)}$

Domain: $\qquad$ Range: $\qquad$
c. $f(x)=\sqrt{(x-2)}+4$

Domain: $\qquad$ Range: $\qquad$
d. $f(x)=\sqrt{2 x}$

Domain: $\qquad$ Range: $\qquad$
e. $f(x)=\sqrt{-x}$

Domain: $\qquad$ Range: $\qquad$
f. $f(x)=-\sqrt{x}$

Domain: $\qquad$ Range: $\qquad$


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## Question 4 ( 6 pts)

a) The below plotted function is the result of applying transformations to a plot of parabola.
I. What is the x -shift? $\qquad$
II. What is the $y$-shift? $\qquad$
III. Find the equation $f(x)$ describing the plot.

IV. What are the zeros of $f(x)$ ? Find these algebraically, not by graph.
b) The graph below describes the function $f\left(\frac{x}{a}\right)$, where 'a' is a number and $\mathrm{f}(\mathrm{x})$ is the function in part (a).
I. What is the value of 'a'? justify your answer.

II. Write explicitly the function $f\left(\frac{x}{a}\right)$, based on the value of 'a' you found and the expression you found for $f(x)$.
III. What are the zeros of the new function? Find these algebraically, not by graph.

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## Question 5 ( 6 pts)

a) Line equation:
I. Find the equation of the line perpendicular to the line

$$
y=3-\frac{x}{2}
$$

and that includes the point $(1,0)$.
II. What is the two lines intersection point? Find it algebraically.
III. Plot the two lines on the graph below.

b) Given the below quadratic function

$$
f(x)=8+x^{2}-4 x
$$

I. Write the quadratic expression in a standard form:
II. Write the function in vertex form:
III. Write the function in factored form:

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## Question 6 ( 6 pts)

The sum of two numbers is 10 .
We define P as the sum of the first number, and the square of the second number.
Find the two numbers such that P is minimum.

## Extra Credit : Question 7 ( 2 pts)

This is NOT meant to be a hard question, and involves very little (if any) calculations. It does require fresh look, and combination of various aspects we learned.

$===$ End of test

